

196(1) : Elliptical orbit from ECE Field Equation
 As in UFT 168 the gravitational field equations are:

$$\underline{\nabla} \cdot \underline{b} = 0 \quad \text{--- (1)}$$

$$\underline{\nabla} \times \underline{g} = \frac{\partial \underline{b}}{\partial t} \quad \text{--- (2)}$$

$$\underline{\nabla} \cdot \underline{d} = \rho_m \quad \text{--- (3)}$$

$$\underline{\nabla} \times \underline{h} - \frac{\partial \underline{d}}{\partial t} = \underline{J}_m \quad \text{--- (4)}$$

where:

$$\underline{d} = \frac{1}{8\pi G} \underline{g} \quad \text{--- (5)}$$

Here \underline{g} is the acceleration due to gravity, \underline{b} is the gravitomagnetic flux density, \underline{d} is the gravitational displacement, \underline{h} is the gravitomagnetic field strength, ρ_m is the mass density and \underline{J}_m is the current of mass density.

These equations are written in a spacetime with torsion and curvature described by a gravitational connection.

The elliptical orbit is the result of neglect of the gravitational connection. In this case:

$$\underline{g} = -\underline{\nabla} \Phi \quad \text{--- (6)}$$

where Φ is the scalar potential of gravitation.

2) In order to obtain an ellipse, the potential must be:

$$\Phi = - \frac{GM}{r} \quad - (7)$$

So $F = mg = - \frac{mMG}{r^2} \quad - (8)$

The ellipse is obtained from the equation:

$$\frac{d^2}{d\theta^2} \left(\frac{1}{r} \right) + \frac{1}{r} = - \frac{mr^2}{L^2} F(r) \quad - (9)$$

where L is the conserved total angular momentum.

From eqs. (8) and (9):

$$r = \frac{d}{1 + e \cos \theta} \quad - (10)$$

where $d = \frac{L^2}{Gm^2 M} \quad - (11)$

Therefore the ellipse is obtained from eq. (3) if the spin correction is neglected.

The observed orbit however is a precessing ellipse:

$$r = \frac{d}{1 + e \cos x\theta} \quad - (12)$$

and its force law is a combination of inverse square and inverse cube terms. The next note will be due to a particular spin correction.