

===== Title

Spherically symmetric line element

===== Coordinates x[0], x[1], x[2], x[3] =

t

r

ϑ

φ

===== Metric g =

$$\begin{pmatrix} \frac{\mu}{r} + 1 & 0 & 0 & 0 \\ 0 & \frac{1}{r+\mu} & 0 & 0 \\ 0 & 0 & r^2 & 0 \\ 0 & 0 & 0 & r^2 \sin^2 \vartheta \end{pmatrix}$$

===== Contravariant Metric gContr =

$$\begin{pmatrix} \frac{r}{r+\mu} & 0 & 0 & 0 \\ 0 & r+\mu & 0 & 0 \\ 0 & 0 & \frac{1}{r^2} & 0 \\ 0 & 0 & 0 & \frac{1}{r^2 \sin^2 \vartheta} \end{pmatrix}$$

===== Christoffel Connection Gamma

$\Gamma[0,0,1] =$

$$-\frac{\mu}{2 r (r + \mu)}$$

$\Gamma[0,1,0] =$

$$-\frac{\mu}{2 r (r + \mu)}$$

$\Gamma[1,0,0] =$

$$\frac{\mu (r + \mu)}{2 r^3}$$

$\Gamma[1,1,1] =$

$$\frac{\mu}{2 r (r + \mu)}$$

$\Gamma[1,2,2] =$

$$-(r + \mu)$$

$\Gamma[1,3,3] =$

$$-(r + \mu) \sin^2 \vartheta$$

$\Gamma[2,1,2] =$

$$\frac{1}{r}$$

$\Gamma[2,2,1] =$

$$\frac{1}{r}$$

1

$$\Gamma[2,3,3] = -\cos\vartheta \sin\vartheta$$

$$\Gamma[3,1,3] = \frac{1}{r}$$

$$\Gamma[3,2,3] = \frac{\cos\vartheta}{\sin\vartheta}$$

$$\Gamma[3,3,1] = \frac{1}{r}$$

$$\Gamma[3,3,2] = \frac{\cos\vartheta}{\sin\vartheta}$$

===== Metric compatibility
===== o.k.

===== Riemann Tensor

$$R[0,1,0,1] = -\frac{\mu}{r^2 (r + \mu)}$$

$$R[0,1,1,0] = \frac{\mu}{r^2 (r + \mu)}$$

$$R[0,2,0,2] = \frac{\mu}{2 r}$$

$$R[0,2,2,0] = -\frac{\mu}{2 r}$$

$$R[0,3,0,3] = \frac{\mu \sin^2\vartheta}{2 r}$$

$$R[0,3,3,0] = -\frac{\mu \sin^2\vartheta}{2 r}$$

$$R[1,0,0,1] = \frac{\mu (r + \mu)}{r^4}$$

$$R[1,0,1,0] = -\frac{\mu (r + \mu)}{r^4}$$

$$R[1,2,1,2] = \frac{\mu}{2 r}$$

$$R[1,2,2,1] = -\frac{\mu}{2 r}$$

$$\begin{aligned}
R[1,3,1,3] &= \frac{\mu \sin^2 \vartheta}{2 r} \\
R[1,3,3,1] &= -\frac{\mu \sin^2 \vartheta}{2 r} \\
R[2,0,0,2] &= -\frac{\mu (r + \mu)}{2 r^4} \\
R[2,0,2,0] &= \frac{\mu (r + \mu)}{2 r^4} \\
R[2,1,1,2] &= -\frac{\mu}{2 r^2 (r + \mu)} \\
R[2,1,2,1] &= \frac{\mu}{2 r^2 (r + \mu)} \\
R[2,3,2,3] &= -\frac{\mu \sin^2 \vartheta}{r} \\
R[2,3,3,2] &= \frac{\mu \sin^2 \vartheta}{r} \\
R[3,0,0,3] &= -\frac{\mu (r + \mu)}{2 r^4} \\
R[3,0,3,0] &= \frac{\mu (r + \mu)}{2 r^4} \\
R[3,1,1,3] &= -\frac{\mu}{2 r^2 (r + \mu)} \\
R[3,1,3,1] &= \frac{\mu}{2 r^2 (r + \mu)} \\
R[3,2,2,3] &= \frac{\mu}{r} \\
R[3,2,3,2] &= -\frac{\mu}{r}
\end{aligned}$$

===== Ricci Tensor
===== all elements zero

===== Ricci Scalar

$R_{sc} =$	0
===== Bianchi identity (Ricci cyclic equation $R \wedge q = 0$)	
===== o.k.	
===== Einstein tensor	
===== all elements zero	
===== Bianchi identity of Hodge dual	
===== (see charge and current densities)	
===== Scalar charge density	
$\rho =$	0
===== Current density class 1	
J[1] =	0
J[2] =	0
J[3] =	0
===== Current density class 2	
J[1] =	0
J[2] =	0
J[3] =	0
===== Current density class 3	
J[1] =	0
J[2] =	0
J[3] =	0